



**Math Virtual Learning**

**Math 8**

**Parallel Lines Cut by a Transversal**

**April 13, 2020**



Lesson: April 13th, 2020

**Objective/Learning Target:**

Students will solve problems involving parallel lines cut by a transversal.

# Warm Up: Vocabulary

## Defined

Parallel Line - lines that never intersect

Transversal - a line that intersects the parallel lines

Vertical Angles - angles that share a vertex but no sides

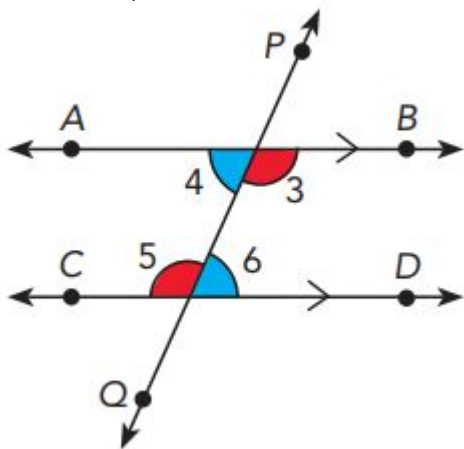
## Matching

- |                  |               |
|------------------|---------------|
| 1. Alternate     | A. Related to |
| 2. Interior      | B. Outside    |
| 3. Exterior      | C. Same       |
| 4. Corresponding | D. Inside     |
| 5. Congruent     | E. Different  |

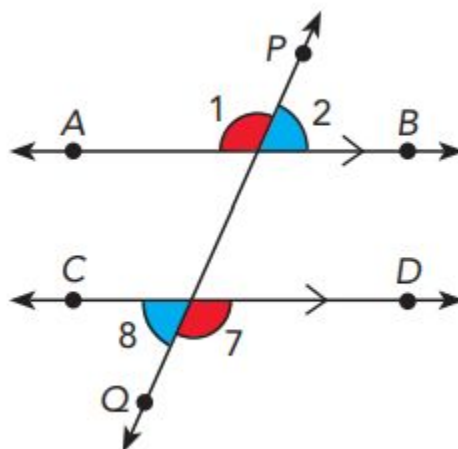
Answers: 1E, 2D, 3B, 4A, 5C

# Guided Practice

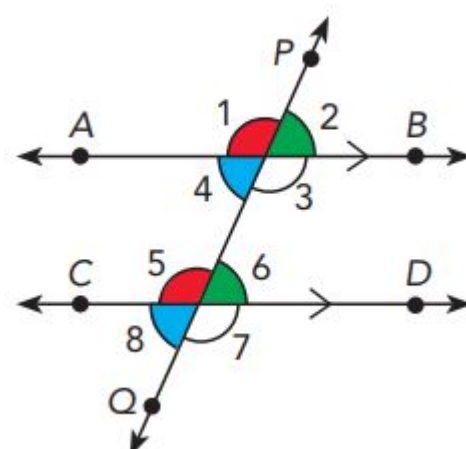
**Alternate Interior Angles** are on **opposite** sides of the transversal and **inside** the parallel lines



**Alternate Exterior Angles** are on **opposite** sides of the transversal and **outside** the parallel lines



**Corresponding Angles** are in the same location if reference to the transversal and their parallel line



**Vertical Angles** share a vertex but no sides  
Red and white angles and  
blue and green angles

# Guided Practice

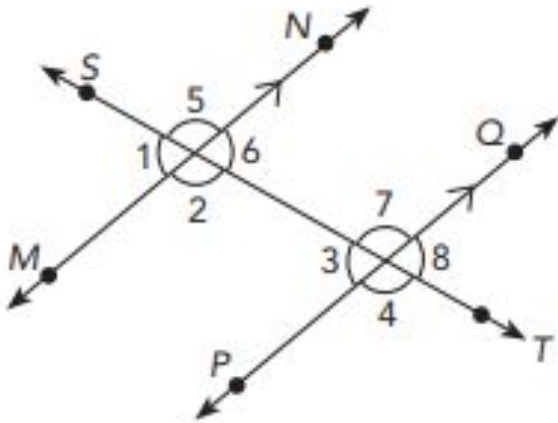
List 2 pairs of each type of congruent angles

Alternate Interior Angles -  $\angle 6$  &  $\angle 3$  and

Alternate Exterior Angles -  $\angle 1$  &  $\angle 8$  and

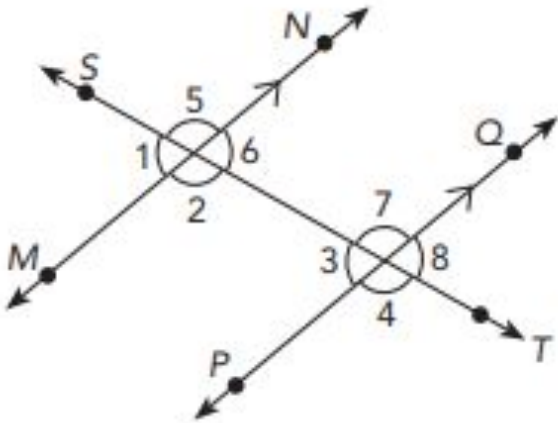
Corresponding Angles -  $\angle 2$  &  $\angle 4$  and

Vertical Angles -  $\angle 3$  &  $\angle 8$  and



# Guided Practice

List 2 pairs of each type of congruent angles



Alternate Interior Angles -  $\angle 6$  &  $\angle 3$  and  $\angle 2$  &  $\angle 7$

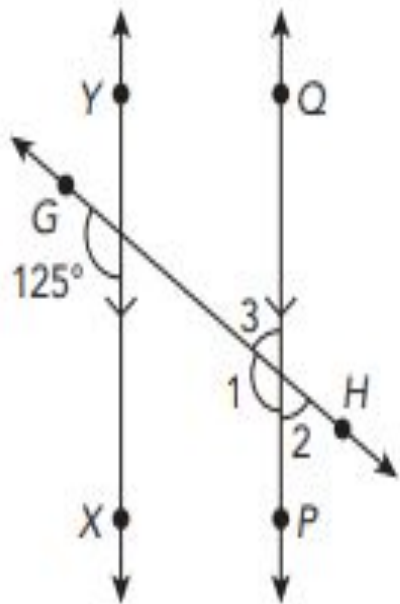
Alternate Exterior Angles -  $\angle 1$  &  $\angle 8$  and  $\angle 5$  &  $\angle 4$

Corresponding Angles -  $\angle 2$  &  $\angle 4$  and  
 $\angle 1$  &  $\angle 3$  or  $\angle 5$  &  $\angle 7$  or  $\angle 6$  &  $\angle 8$

Vertical Angles -  $\angle 3$  &  $\angle 8$  and  
 $\angle 7$  &  $\angle 4$  or  $\angle 1$  &  $\angle 6$  or  $\angle 5$  &  $\angle 2$

# Guided Practice

In the diagram,  $\overline{XY}$  is parallel to  $\overline{PQ}$ . Find the measures of  $\angle 1$ ,  $\angle 2$ , and  $\angle 3$ .



$$m\angle 1 = \underline{\hspace{2cm}}$$

Corr.  $\angle$ s

$$m\angle 1 + m\angle 3 = \underline{\hspace{2cm}}$$

Supp.  $\angle$ s

$$\underline{\hspace{2cm}} + m\angle 3 = \underline{\hspace{2cm}}$$

Substitute  $m\angle 1 = \underline{\hspace{2cm}}$ .

$$m\angle 3 + \underline{\hspace{2cm}} - 125^\circ = \underline{\hspace{2cm}} - 125^\circ \quad \text{Subtract } 125^\circ \text{ from both sides.}$$

$$m\angle 3 = \underline{\hspace{2cm}}$$

Simplify.

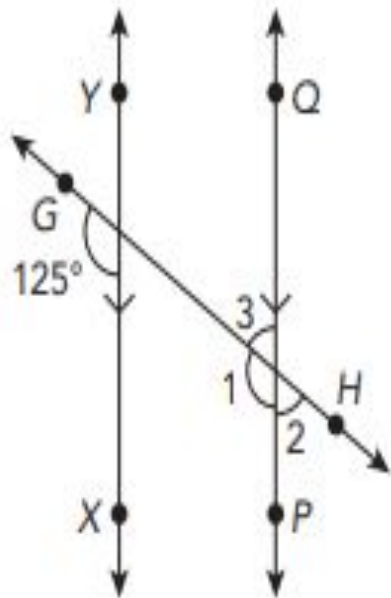
$$m\angle 3 = \underline{\hspace{2cm}}$$

Vert.  $\angle$ s

$$= \underline{\hspace{2cm}}$$

# Guided Practice

In the diagram,  $\overline{XY}$  is parallel to  $\overline{PQ}$ . Find the measures of  $\angle 1$ ,  $\angle 2$ , and  $\angle 3$ .



$$m\angle 1 = \underline{125^\circ}$$

Corr.  $\angle$ s

$$m\angle 1 + m\angle 3 = \underline{180^\circ}$$

Supp.  $\angle$ s

$$\underline{125^\circ} + m\angle 3 = \underline{180^\circ}$$

Substitute  $m\angle 1 = \underline{125^\circ}$

$$m\angle 3 + \underline{125^\circ} - 125^\circ = \underline{180^\circ} - 125^\circ$$

Subtract  $125^\circ$  from both sides.

$$m\angle 3 = \underline{55^\circ}$$

Simplify.

$$m\angle 3 = \underline{m\angle 2}$$

Vert.  $\angle$ s

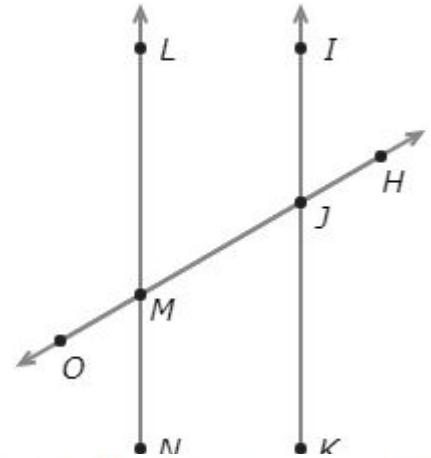
$$= \underline{55^\circ}$$



## Practice:

Click the link below for additional practice on:  
[Transversals of Parallel Lines: Find Angle Measures](#)

Look at this diagram:



1. Apply what you have learned about angle relationships when parallel lines are cut by a transversal to complete the given practice problems.
2. Enter your answer in the given box.
3. Press submit for feedback to see how you are doing.

If  $\overleftrightarrow{IK}$  and  $\overleftrightarrow{LN}$  are parallel lines and  $m\angle LMJ = 60^\circ$ , what is  $m\angle IJH$ ?

Click here to check  
your answer

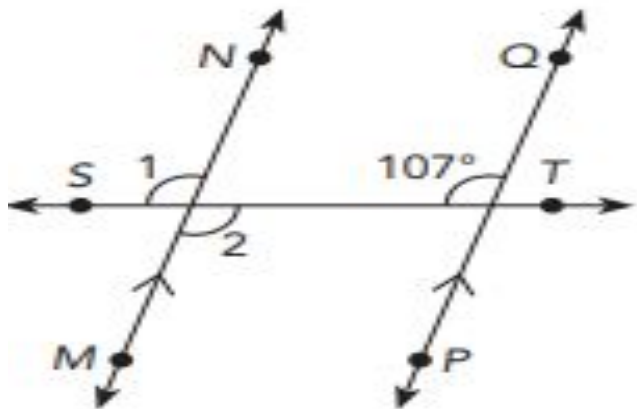
Submit

# Independent Practice:

Work through the following examples on a separate piece of paper.

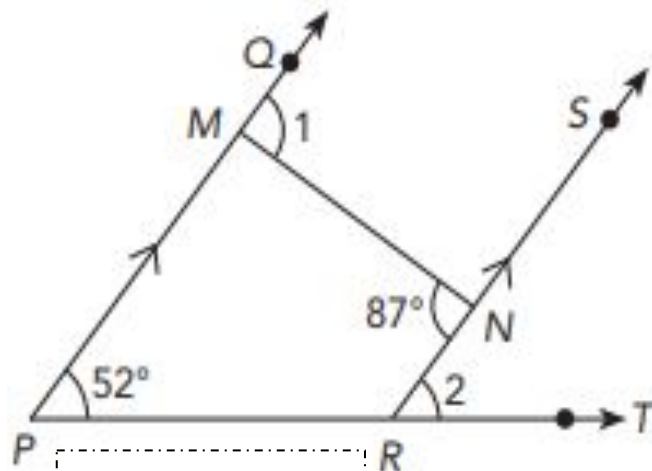
Find the measure of each numbered angle.

1.  $\overrightarrow{MN}$  is parallel to  $\overrightarrow{PQ}$ .



$m\angle 1 = \underline{\hspace{1cm}}^\circ$   
 $m\angle 2 = \underline{\hspace{1cm}}^\circ$

2.  $\overrightarrow{PQ}$  is parallel to  $\overrightarrow{RS}$ .



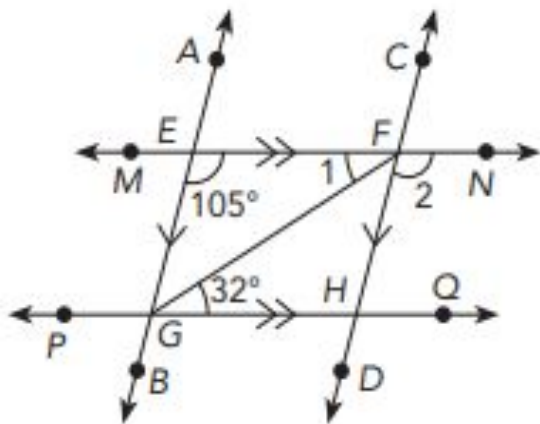
$m\angle 1 = \underline{\hspace{1cm}}^\circ$   
 $m\angle 2 = \underline{\hspace{1cm}}^\circ$

# Independent Practice:

Work through the following examples on a separate piece of paper.

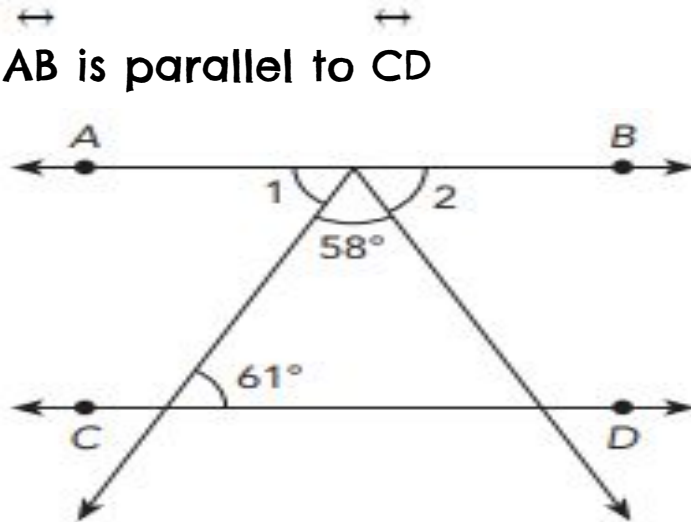
Find the measure of each numbered angle.

3.  $\overleftrightarrow{AB}$  is parallel to  $\overleftrightarrow{CD}$  and  $\overleftrightarrow{MN}$  is parallel to  $\overleftrightarrow{PQ}$ .



$m\angle 1 = \underline{\hspace{1cm}}^\circ$   
 $m\angle 2 = \underline{\hspace{1cm}}^\circ$

4.  $\overleftrightarrow{AB}$  is parallel to  $\overleftrightarrow{CD}$



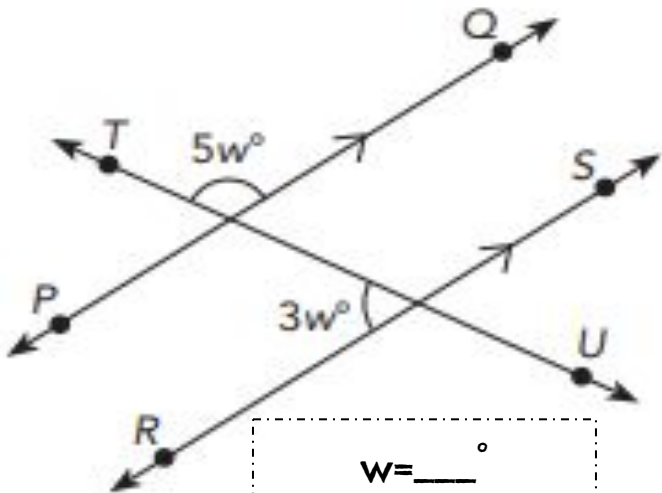
$m\angle 1 = \underline{\hspace{1cm}}^\circ$   
 $m\angle 2 = \underline{\hspace{1cm}}^\circ$

# Independent Practice:

Work through the following examples on a separate piece of paper.

Find the value of each variable.

5.  $\overline{PQ}$  is parallel to  $\overline{RS}$ .

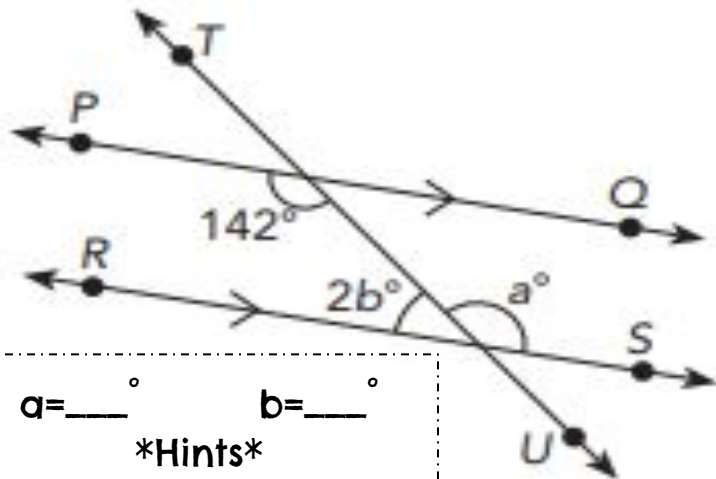


$$w = \underline{\hspace{1cm}}^\circ$$

\*Hint\*

$$5w^\circ + 3w^\circ = 180^\circ$$

6.  $\overline{PQ}$  is parallel to  $\overline{RS}$ .



$$a = \underline{\hspace{1cm}}^\circ \quad b = \underline{\hspace{1cm}}^\circ$$

\*Hints\*

$a^\circ$  is an alternate interior angle with  $142^\circ$

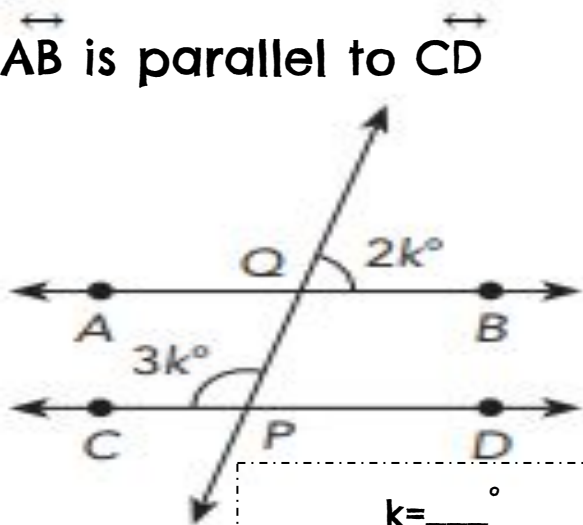
$$2b^\circ + a^\circ = 180^\circ$$

# Independent Practice:

Work through the following examples on a separate piece of paper.

Find the value of each variable.

7.  $\overleftrightarrow{AB}$  is parallel to  $\overleftrightarrow{CD}$

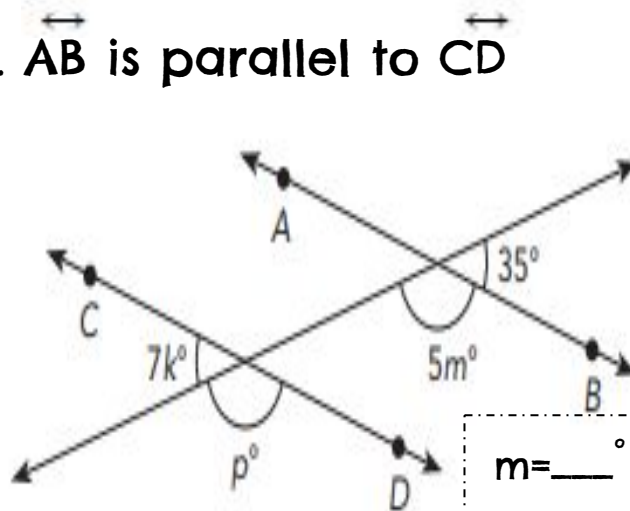


$$k = \underline{\hspace{1cm}}^\circ$$

**\*Hints\***

$$m\angle QPD = k^\circ$$
$$3k^\circ + 2k^\circ = 180^\circ$$

8.  $\overleftrightarrow{AB}$  is parallel to  $\overleftrightarrow{CD}$



$$m = \underline{\hspace{1cm}}^\circ \quad p = \underline{\hspace{1cm}}^\circ \quad k = \underline{\hspace{1cm}}^\circ$$

**\*Hints\***

$$5m^\circ + 35^\circ = 180^\circ$$

$$p^\circ = 5m^\circ$$

$$7k^\circ + p^\circ = 180^\circ$$

# Independent Practice **Answer Key:**

Once you have completed the problems, check your answers here.

Find the measure of each numbered angle.

1.

$$m\angle 1 = 107^\circ$$
$$m\angle 2 = 107^\circ$$

2.

$$m\angle 1 = 32^\circ$$
$$m\angle 2 = 105^\circ$$

3.

$$m\angle 1 = 87^\circ$$
$$m\angle 2 = 52^\circ$$

4.

$$m\angle 1 = 61^\circ$$
$$61 + m\angle 2 + 58 = 180$$
$$m\angle 2 + 119 = 180$$
$$\quad -119 \quad -119$$
$$m\angle 2 = 61^\circ$$

# Independent Practice **Answer Key:**

Once you have completed the problems, check your answers here.

Find the value of each variable.

5.

$$w = \mathbf{22.5^\circ}$$

$$5w^\circ + 3w^\circ = 180^\circ$$

$$\frac{8w^\circ}{8} = \frac{180^\circ}{8}$$

$$w = 22.5^\circ$$

$$w = 22.5^\circ$$

6.

$$a = \mathbf{142^\circ}$$

$$b = \mathbf{19^\circ}$$

$$2b^\circ + a^\circ = 180^\circ$$

$$2b^\circ + 142 = 180^\circ$$

$$-142 \quad -142$$

$$\frac{2b^\circ}{2} = \frac{38^\circ}{2}$$

$$b = 19^\circ$$

$$b = 19^\circ$$

# Independent Practice **Answer Key:**

Once you have completed the problems, check your answers here.

Find the value of each variable.

7. AB is parallel to CD

$$k = 36^\circ$$

$$3k^\circ + 2k^\circ = 180^\circ$$

$$\frac{5k^\circ}{5} = \frac{180^\circ}{5}$$

$$k^\circ = 36^\circ$$

8. AB is parallel to CD

$$m = 29^\circ \quad p = 145^\circ \quad k = 5^\circ$$

$$5m^\circ + 35^\circ = 180^\circ$$

$$\frac{5m^\circ}{5} = \frac{145^\circ}{5}$$

$$m^\circ = 29^\circ$$

$$7k^\circ + p^\circ = 180^\circ$$

$$7k^\circ + 145^\circ = 180^\circ$$

$$\frac{7k^\circ}{7} = \frac{35^\circ}{7}$$

$$k = 5^\circ$$

$$p^\circ = 5m^\circ$$

$$p^\circ = 5(29)$$

$$p^\circ = 145^\circ$$



## **Additional Practice:**

[Math is Fun: Parallel Lines and Pairs of Angles](#)

[Khan Academy-Angle Relationships with Parallel Lines](#)

[Khan Academy- Equation Practice with Angles](#)

[Math Games-Transversal of Parallel Lines](#)

[Math Planet-Quick Video Explanation](#)